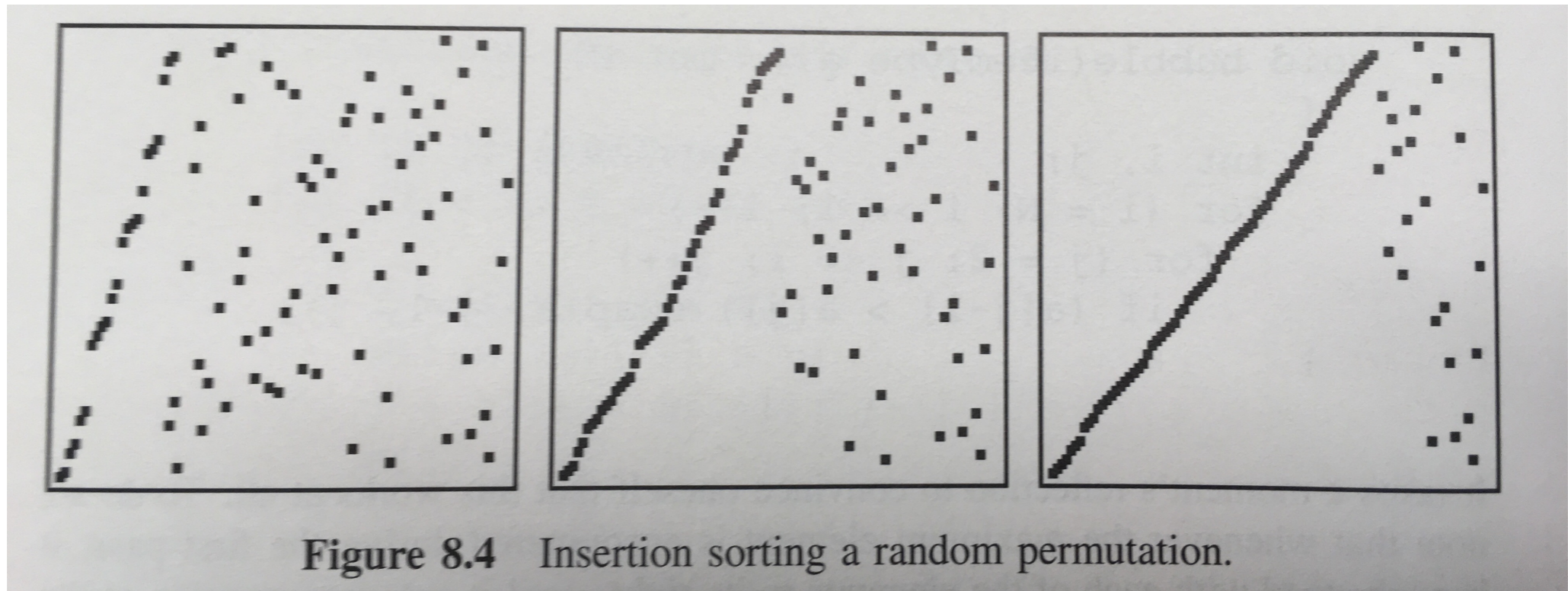


Sorting Algorithms

Part 1

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Value on y axis, index on x axis. From Sedgewick "Algorithms in C++"

Overview and Rules

- We talk about sorting **files** of **records**.
- Records may be quite complex, so sort actually operates on simpler **keys**.
- Sorts re-arrange sets of keys
 - e.g. numerical or alphabetical order.

- This gives us the elegant representation:

input **instance** $S = \{9, 2, 3, 8\}$

sorting algorithm goes to work in here

output **permutation** $S' = \{2, 3, 8, 9\}$

- We can `.`: use arrays of integers to represent keys in our demos.
- Can swap sorting functions to compare on same arrays.
- Consider an **indirect sort** to avoid shuffling v. large data (sort array of pointers instead).

Stability

- A sorting algorithm is **stable** if it preserves original order of equal-value keys
- e.g. records show student names originally in alphabetical order. but keys are based on grades.
- Elementary sorts are usually stable.
- Sophisticated sorts are usually unstable.
- Can modify key. Turns out to be quite tricky or expensive.

Elementary Sorts

- We will start with simple 'elementary sorts'
 - sometimes these are the best choice for bigger problems
 - start with simple problems to learn general ideas
- Try to build functions that implement all of these: good practise
- Build a table comparing time and space complexity
- Know special pros and cons of each beyond complexity

Elementary Sorts

- Properties
 - Usually take N^2 steps to sort N items \therefore bad on big data sets
 - Simple to implement
 - May actually be quicker on mostly-sorted data
- Selection sort
- Insertion sort
- Bubble sort
- Shell sort - *can be a great choice on random data*

Selection Sort Algorithm

- *"select the smallest remaining element"*
- Given set **S** of **n** values
- **Loop** over array from left to right (`array[0]` to `array[n-2]`)
 - **Loop** over rest of array (**[current_index]** to **[n-1]**) looking for smallest value
 - **Swap** `array[current_index]` and `array[min_index]`
- Blackboard walk-through here
- Live coding demo here...

Selection Sort

- Ease of implementation?
- Time complexity avg., best, worst $O(\dots)$?
- Space complexity base $O(\dots)$? and *auxiliary* (amount of extra space used whilst working).
- Why is this *stable*? hint: one operation
- Bad for?
- Good for?
 - consider that every item is moved max once.

Aside on Unix-style programs

- Why are we talking about sorting records within files?
- It usually **is** a file with a series of lines as records
 - text list of strings
 - csv or spreadsheet — maybe grades are the key
- If you print the output to the console e.g. `printf`
- redirect printed output to a new file
 - `./mysort input.csv > output.csv`
- can also chain wee programs together with pipes |
 - `./mysort input.csv | ./mycsv2json > output.json`

Insertion Sort Algorithm

- *"insert new card into already sorted hand of cards"*
- start at left of array and loop once to right
 - check new card to the right of current card
 - if it's smaller than current card swap them over
 - this should loop all the way back to the left e.g.
 $S = \{2,3,4,\mathbf{5},1\}$
- imagine our current card is the 5
- Idea how to code this?

```

for ( int pass = 0; pass < length - 1; pass++ ) {
    for ( int i = pass + 1; i > 0; i-- ) {
        if ( array[i - 1] > array[i] ) {
            int temp = array[i];
            array[i] = array[i - 1];
            array[i - 1] = temp;
        } else {
            break;
        }
    }
}

```

- Loop over array length -1
- Nested loop goes **backwards** from next element to [1]
- Compare current and next elements
- If next is smaller, do a swap and continue left
- Otherwise break and continue main loop right

Insertion Sort

- Time and space complexity?
- Other advantages
 - one at a time input
 - implementation simple

Bubble Sort Algorithm

- sorted = false
- while (sorted == false)
 - sorted = true
 - loop over data
 - if (next < current)
 - swap(current, next)
 - sorted = false

Bubble Sort

- Time and space complexity? Worst, average, **best**?
- Advantages:
 - Code is simple
 - Can stop early if numbers already sorted
 - No other sorting algorithm does this
 - Can do one run to check before calling complex sorting algorithm
 - "Stable"
- *Sedgewick has a different algorithm called Bubble Sort
- Computer scientists have very negative things to say about Bubble Sort's worst case performance vs Insertion Sort.

Summary - Elementary Sorting Algorithms

- Very simple to implement. Also interchangeable. Some useful properties.
- $O(n^2)$ worst case time
 - May not play well with cache - try them with a timer
- $O(1)$ auxiliary memory (1 variable for swapping)
- Stable